# ПAmIBIA UחIVERSITY OF SCIEПCE AПD TECHחOLOGY 

 Faculty of Health and Applied SciencesDepartment of Mathematics and Statistics

| QUALIFICATION: Bachelor of Technology: Accounting and Finance, Advanced Diploma in the <br> Theory of Accounting, Bachelor of Accounting and Diploma in Accounting and Finance |  |
| :--- | :--- |
| QUALIFICATION CODE: 23BACF ;07BACP; <br> 06BDAF; 07ADTA | LEVEL: 5 |
| COURSE: QUANTITATIVE METHODS | COURSE CODE: QTM511S |
| SESSION: June 2019 | PAPER: THEORY |
| DURATION: 3 Hours | MARKS: 100 |


| FIRST OPPORTUNITY EXAMINATION QUESTION PAPER |  |
| :--- | :--- |
| EXAMINER(S) | Mr. A Roux; Ms. S Mwewa; Dr. G Dibaba; Dr. D Ntirampeba |
| MODERATOR: | Mr. J Swartz |


| INSTRUCTIONS |
| :--- | :--- |
| 1. Answer ALL the questions. |
| 2. Write clearly and neatly. |
| 3. Number the answers clearly. |

## PERMISSIBLE MATERIALS

1. Non-Programmable Calculator without the cover

## ATTACHMENTS

2. Formula Sheet

THIS QUESTION PAPER CONSISTS OF 4 PAGES INCLUDING THIS FRONT PAGE (Excluding the formula sheet)
1.1) The following table shows the number of pedestrians involved in serious road accidents in Windhoek during the years 2008-2018.

| Year | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 | 2018 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Nr.Pedestrians | 33 | 30 | 35 | 31 | 34 | 30 | 33 | 35 | 33 | 36 | 39 |  |

1.1.1) Plot the time series data.
1.1.2) Determine the least squares trend line equation, using the sequential coding method to code the time variable. Start your coding for the first period (2008) as 1.
1.1.3) Estimate the number of pedestrians involved in serious road accidents in Windhoek 2021
(3)
1.2) Given the following prices and quantities:

| Price (per kg) |  |  |  | Quantities produced |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2008 | 2013 | 2018 | 2008 | 2013 | 2018 |
| Milk | 3.95 | 3.89 | 4.13 | 675 | 717 | 436 |
| Cheese | 61.50 | 62.20 | 59.70 | 117 | 115 | 115 |
| Butter | 34.80 | 35.40 | 38.90 | 77 | 74 | 82 |

1.2.1) Compute and interpret the Laspeyres price index number for the year 2018 with 2008 as base.
1.2.2) Compute and interpret the Paasche's price index number for the year 2018 with 2008 as base.

## QUESTION 2 [11]

2.1) An amount was invested on Jan 1, 2015 such that it generated a periodic payment of $N \$ 2000$ at the end of each month of the calendar year 2015. The annually interest rate on the investment was $13.2 \%$. What was the original investment?
2.2) Patrick recently purchased a car for $N \$ 45000$ and decided to finance the car by obtaining a car loan from FNB, payable at the end of each month for 4 years at an annual interest rate of $12.90 \%$. Determine Patrick's monthly payments on the loan.(5)

During one month, time records shows the following results for the number of production workers absent per day:

| 13 | 14 | 9 | 17 | 21 | 10 | 15 | 22 | 19 | 13 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 22 | 13 | 19 | 23 | 17 | 21 | 10 | 9 | 20 | 18 |

For the distribution above, calculate and interpret the:
3.1) Range
3.2) Mode
3.3) Median
3.4) Arithmetic mean
3.5) Variance
3.6) Standard deviation
3.7) Coefficient of variation

## QUESTION 4 [15]

The Office of The Bursar at The Namibia University of Science and Technology (NUST) revealed some information regarding method of payment for a group of 2000 students at different levels of study.

|  | Bursary | Loan | Self | Totals |
| :--- | :--- | :--- | :--- | :--- |
| Certificate | 12 | 379 | 727 | $\mathbf{1 1 1 8}$ |
| Diploma | 39 | 106 | 642 | $\mathbf{7 8 7}$ |
| Degree | 48 | 20 | 57 | $\mathbf{9 5}$ |
| Totals | $\mathbf{6 9}$ | $\mathbf{5 0 5}$ | $\mathbf{1 4 2 6}$ | $\mathbf{2 0 0 0}$ |

4.1) Find the probability of randomly selecting one student from this group who pays for him/herself?
4.2) Find the probability of randomly selecting one student from this group who has a Diploma or a Degree?
4.3) Find the probability of randomly selecting one student from this group who has a Bursary or Degree?
4.4) What is the chance of randomly selecting one student with a degree, given that this student has a loan?

## QUESTION 5 [22]

5.1) A person plans to deposit one sixth of a monthly salary of $N \$ 7200$ at the end of every month for three years into an account paying interest at the rate of $4 \%$ compounded monthly. Determine how much will be in the account at the end of the three years. (4)
5.2) Jonas takes out a loan of $N \$ 100000$ at $9 \%$ p.a. simple interest to finance his study at NUST for 7 years. He won a prize and decided to repay N\$ 20000 after 3 years, N\$ 45000 after a further two years and a further $N \$ 16000$ after a further year. What is the amount outstanding of seven years after the loan was taken out?
5.3) Solve the following system of linear equations. Is the solution unique? Explain.

$$
\begin{aligned}
& 2 x+2 y-2 z=-4 \\
& -2 x+y-z=-5 \\
& x-2 y-2 z=-1
\end{aligned}
$$

5.4) Solve and represent on the number line the following inequality.

$$
4(3 x+20) \leq 50
$$

XXXXXXXXXXXXXX END OF EXAMINATION XXXXXXXXXXXXX

## SUMMARY OF FORMULAE QTM511S

## JUNE/July 2018 EXAM

Simple Interest:

$$
I=P r t
$$

Compound Interest:

$$
A=P(1+i)^{n}
$$

Effective Interest Rate

$$
r_{e f f}=\frac{r}{1-r t}
$$

Effective Interest Rate $\quad r_{e f f}=\left(1+\frac{r}{m}\right)^{m}-1$
Discount

$$
P=A(1-d t) \quad D=A d t
$$

Simple discount Rate $\quad d=\frac{r}{1+r t}$

Nominal Interest Rate

$$
r=m\left[\left(1+r_{e f f}\right)^{\frac{1}{m}}-1\right]
$$

Ordinary Annuity Certain Ordinary Annuity Certain
$S_{n}=R\left[\frac{\left(1+\frac{r}{m}\right)^{n}-1}{\frac{r}{m}}\right]$
$A_{n}=R\left[\frac{1-\left(1+\frac{r}{m}\right)^{-n}}{\frac{r}{m}}\right]$

Period $t=\frac{\log S-\log P}{m \log \left(1+\frac{r}{m}\right)}$

$$
n=\frac{\log 2}{\log \left(1+\frac{r}{m}\right)}
$$

$$
t=\frac{N-1}{r} \text { for } N \geq 2 n=\frac{\log \left(\frac{i S_{n}}{R}+1\right)}{\log (1+i)} \quad n=-\frac{\log \left(1-\frac{i A_{n}}{R}\right)}{\log (1+i)}
$$

## Measures of Central Tendency

Mean $\bar{x}=\frac{\sum x}{n} \quad \bar{x}=\frac{\sum f x}{\sum f}$

Median

$$
M_{d}=l_{M d}+h\left(\frac{\frac{n}{2}-F}{f}\right)
$$

Mode

$$
M_{0}=l_{M o}+h\left[\frac{f_{1}-f_{o}}{\left(f_{1}-f_{o}\right)+\left(f_{1}-f_{2}\right)}\right],
$$

## Measures of dispersion

Variancé $=\frac{\sum f^{2}-n(\bar{x})^{2}}{n-1}$ or $\quad$ Variance $=\frac{\sum(x-\bar{x})^{2}}{n-1} \quad$ coefficient of variation $=\left(\frac{S}{\bar{x}}\right) \times 100$
Standard deviation $=\sqrt{\text { variance }}$
Quartile

$$
M_{k}=l+\frac{h}{f}\left(\frac{k n}{4}-F\right)
$$

## Index Numbers

Laspeyres price index $=\frac{\sum\left(P_{i} \times Q_{b}\right)}{\sum\left(P_{b} \times Q_{b}\right)} \times 100 \% \quad$ Paasche price index $=\frac{\sum\left(P_{i} \times Q_{i}\right)}{\sum\left(P_{b} \times Q_{i}\right)} \times 100 \%$
Laspeyres quantity index $=\frac{\sum\left(P_{b} \times Q_{i}\right)}{\sum\left(P_{b} \times Q_{b}\right)} \times 100 \% \quad$ Paasche quantity index $=\frac{\sum\left(P_{i} \times Q_{i}\right)}{\sum\left(P_{i} \times Q_{b}\right)} \times 100 \%$

## Time Series

$\hat{y}=a+b x \quad b=\frac{n \sum x y-\sum x \sum y}{n \sum x^{2}-\left(\sum x\right)^{2}} \quad a=\frac{\sum y-b \sum x}{n}$

## Probability

$P(A \cup B)=P(A)+P(B)-P(A \cap B) \quad P(A \cap B)=P(A) P(B)$
$\dot{P}(B \mid A)=\frac{P(A \cap B)}{P(A)}$,

